# RELATIONSHIPS BETWEEN <br> STRUCTURE AND CARBONYL STRETCHING FREQUENCIES OF THE $\beta$-LACTAM RING AND THE <br> 7-ACYLAMINO GROUP IN 1-THIAAND 1-OXA-CEPHEM ANTIBIOTICS. IMPORTANCE OF THE BENDING <br> ANGLE OF THE C(4)-N(5) BOND <br> FROM PLANE C(6)-N(5)-C(8) <br> IN THE $\beta$-LACTAM RING 

Sir:
The useful antibacterial activity arising from the $\beta$-lactam ring in $\beta$-lactam antibiotics has attracted much attention ${ }^{11}$. The $\beta$-lactam IR stretching frequency ( $\beta$-lactam $\nu_{\mathrm{c}=0}$ ) has been regarded as an important index for investigating the struc-ture-activity relationship of the $\beta$-lactam antibiotics ${ }^{2 \sim 5}$. However, only a few studies have focused attention on the change in the $\beta$-lactam $\nu_{\mathrm{c}=0}$ in the cases of replacement of the $7 \alpha$-hydrogen atom by a methoxy group and that of the sulfur by an oxygen atom at the 1 -position of cephalo-


|  | A | X | Y | Z | R |
| :---: | :--- | :--- | :--- | :--- | :--- |
| $\mathbf{1}$ | O | H | Tet | $\mathrm{COOCHPh}_{2}$ | Ph |
| $\mathbf{2}$ | S | H | Tet | $\mathrm{COOCHPh}_{2}$ | Ph |
| $\mathbf{3}$ | O | OMe | Tet | $\mathrm{COOCHPh}_{2}$ | Ph |
| $\mathbf{4}$ | S | OMe | Tet | $\mathrm{COOCHPh}_{2}$ | Ph |
| $\mathbf{9}$ | O | H | Tet | COONa | $\mathrm{CH}_{2} \mathrm{Ph}$ |
| $\mathbf{1 0}$ | S | H | Tet | COONa | $\mathrm{CH}_{2} \mathrm{Ph}$ |
| $\mathbf{1 1}$ | O | OMe | Tet | COONa | $\mathrm{CH}_{2} \mathrm{Ph}$ |
| $\mathbf{1 2}$ | S | OMe | Tet | COONa | $\mathrm{CH}_{2} \mathrm{Ph}$ |
| $\mathbf{1 3}$ | O | H | H | COONa | $\mathrm{CH}_{2} \mathrm{Ph}$ |
| $\mathbf{1 4}$ | S | H | H | COONa | $\mathrm{CH}_{2} \mathrm{Ph}$ |
| $\mathbf{1 5}$ | O | OMe | H | COONa | $\mathrm{CH}_{2} \mathrm{Ph}$ |
| $\mathbf{1 6}$ | S | OMe | H | COONa | $\mathrm{CH}_{2} \mathrm{Ph}$ |
| $\mathbf{1 7}$ | O | H | Tet | $\mathrm{COOCHPh}_{2}$ | $\mathrm{CH}_{2} \mathrm{Ph}$ |
| $\mathbf{1 8}$ | S | H | Tet | COOCHPh | $\mathrm{CH}_{2} \mathrm{Ph}$ |
| $\mathbf{1 9}$ | O | OMe | Tet | $\mathrm{COOCHPh}_{2}$ | $\mathrm{CH}_{2} \mathrm{Ph}$ |
| $\mathbf{2 0}$ | S | OMe | Tet | COOCHPh | $\mathrm{CH}_{2} \mathrm{Ph}$ |
| $\mathbf{2 5}$ | S | H | H | COMe | $\mathrm{CH}_{2} \mathrm{OPh}$ |
| $\mathbf{2 6}$ | S | OMe | H | $\mathrm{COOCMe}_{3}$ | $\mathrm{CH}_{2} \mathrm{Ph}$ |

sporin antibiotics ${ }^{5}$. In the preceding paper ${ }^{8)}$, we presented some $\beta$-lactam $\nu_{\mathrm{c}=0}$ data related to these points, comparing them with ${ }^{13} \mathrm{C}$ NMR and the pseudo-first-order rates of the 3 -cephem $\beta$ lactam ring opening at pH 10 and $35^{\circ} \mathrm{C}, \mathrm{k}_{\text {obs }}$. Further detailed examinations of the $\beta$-lactam $\nu_{\mathrm{C}=0}$ of several cephalosporin derivatives have revealed that the $\nu_{\mathrm{c}=\mathrm{o}}$ values can be correlated with the geometrical structure parameters obtained from X-ray analyses ${ }^{3,7 \sim 11)}$. In order to explain these results theoretically, we also carried out CNDO/2 calculations for simple model compounds.

Table 1 lists the IR and NMR spectral data of the cephalosporin derivatives together with the available structural parameters ${ }^{3,7 \sim 11)}$. The $\beta$ lactam $\nu_{\mathrm{c}=0}$ shifts to a higher wavenumber with an increase in bending angle $\theta$ when the 1 -sulfur atom is replaced by an oxygen atom, but to a lower wavenumber with a decrease in $\theta$ when the $7 \alpha$-hydrogen atom is substituted by a methoxy group. An important factor for these shifts is considered to be a resonance change such as


|  | A | X | Y | Z | R |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 5 | O | H | Tet | ${ }^{\mathrm{H}} \mathrm{COOCHPh}_{2}$ | Ph |
| 6 | S | H | Tet | ${ }^{\mathrm{H}} \mathrm{COOCHPh}_{2}$ | Ph |
| $7$ | O | OMe | Tet | ${ }^{\mathrm{H}} \mathrm{COOCHPh}_{2}$ | Ph |
| 8 | S | OMe | Tet | ${ }^{\mathrm{H}} \mathrm{COOCHPh}_{2}$ | Ph |
| 21 | O | H | Tet | $\stackrel{\mathrm{H}}{\mathrm{COOCHPh}_{2}}$ | $\mathrm{CH}_{2} \mathrm{Ph}$ |
| 22 | S | H | Tet | ${ }^{\mathrm{H}} \mathrm{COOCHPh}_{2}$ | $\mathrm{CH}_{2} \mathrm{Ph}$ |
| 23 | O | OMe | Tet | $\stackrel{\mathrm{H}}{\mathrm{COOCHPh}_{2}}$ | $\mathrm{CH}_{2} \mathrm{Ph}$ |
| 24 | S | OMe | Tet | ${ }^{\mathrm{H}} \mathrm{COOCHPh}_{2}$ | $\mathrm{CH}_{2} \mathrm{Ph}$ |
| 27 | S | H | H | $\stackrel{\mathrm{H}}{\mathrm{COOH}}$ | $\mathrm{CH}_{2} \mathrm{OPh}$ |
| 28 | S | COOMe | H | $\stackrel{\mathrm{COOMe}}{\stackrel{\text { COOMe }}{ }}$ | $\mathrm{CH}_{2} \mathrm{OPh}$ |

Table 1. IR and ${ }^{13} \mathrm{C}$ NMR spectral data and structural parameters of cephalosporin derivatives. ${ }^{a}$

| IR stretching frequency, $\nu_{\mathrm{C}=0}\left(\mathrm{~cm}^{-1}\right)^{c}$ |  |  |  |  |  |  | ${ }^{13} \mathrm{C} \mathrm{NMR}{ }^{\text {d }}$ |  | Structural parameters ${ }^{\text {b }}$ |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Compound No. | $\beta$-Lactam | 7-Amide | Compound No. | $\beta$-Lactam | Compound No. | $\beta$-Lactam | Compound No. | $\delta_{\text {C(8) }}$ | Compound No. | $\theta\left({ }^{\circ}\right)^{e}$ | $\phi_{1}\left({ }^{\circ}\right)^{f}$ | $\phi_{2}\left({ }^{\circ}\right)^{g}$ | Reference |
| 1 | 1797.1 | 1676.0 | 9 | 1778.4 | 13 | 1769.1 | 17 | 168.5 | 17 | 29.6 | 138.7 | $-1.8$ | 11) |
| 2 | 1791.0 | 1678.0 | 10 | 1772.7 | 14 | 1763.7 | 18 | 165.1 | 25 | 20.5 | 118.9 | 2.8 | 7) |
| 3 | 1787.1 | 1688.5 | 11 | 1772.0 | 15 | 1766.7 | 19 | 162.5 | 19 | 21.9 | 74.8 | -12.2 | 8) |
| 4 | 1781.5 | 1684.5 | 12 | 1768.0 | 16 | 1762.3 | 20 | 160.7 | 26 | 14.5 | 69.7 | -7.6 | 9) |
| 5 | 1793.5 | 1676.2 |  |  |  |  | 21 | 167.1 |  |  |  |  |  |
| 6 | 1781.2 | 1675.6 |  |  |  |  | 22 | 163.9 | 27 | 6.7 | 98.4 | -1.6 | 3) |
| 7 | 1789.1 | 1685.6 |  |  |  |  | 23 | 162.1 |  |  |  |  |  |
| 8 | 1778.0 | 1681.6 |  |  |  |  | 24 | 160.3 | $28^{h}$ | $-3.0$ | 71.8 | $-6.9$ | 10) |

## a Compounds $\mathbf{1 \sim 8}$ were kindly supplied by Sendo et al. ${ }^{17 \text { ) }}$

${ }^{b}$ Data on salts are excluded from this list because strong interaction may exist in crystals.
c IR spectra were recorded on a JASCO DS-403G grating spectrometer calibrated in a usual manner. Compounds $\mathbf{1} \sim \mathbf{8}$ were dissolved in $\mathrm{CHCl}_{3}$ at $c a$. 0.002 m (cell length 0.5 cm ). Accuracies of $\nu_{\mathrm{O}=0}$ are within $\pm 1.0 \mathrm{~cm}^{-1}$. Data on compounds $\mathbf{9} \sim \mathbf{1 6}$ are taken from reference 6 .
${ }^{d} \quad{ }^{13} \mathrm{C}$ NMR spectra were recorded and assigned as reported previously ${ }^{66}$.
e Bending angle of $\mathbf{C}(4)$ from plane $C(6) N(5) C(8)$.
$f$ Torsion angle $\mathrm{C}(6) \mathrm{C}(7) \mathrm{N}(10) \mathrm{C}(11)$.

- Torsion angle $\mathrm{C}(7) \mathrm{N}(10) \mathrm{C}(11) \mathrm{O}(12)$.
${ }^{h}$ Data for this molecule were used because of the lack of X-ray crystallographic data on appropriate analogous compounds.

Table 2. Bond lengths $(\AA)$, bond angles $\left({ }^{\circ}\right)^{3,7 \sim 11,13 \sim 18)}$ and model molecules used in CNDO/2 calculations.

${ }^{a}$ The assumptions were made that all atoms of the $\beta$-lactam ring lie on the same plane and that the atoms connected to the $\beta$-lactam ring are located in the bisectional plane of the respective endocyclic bond angle.
${ }^{b}$ The $\mathrm{H}_{\mathrm{a}}$ atom of the Me group is placed in the bisectional plane of angle $\mathrm{C}(2) \mathrm{N}(1) \mathrm{C}(4)$, and the plane of the $\mathrm{CH}=\mathrm{CH}_{2}$ group is perpendicular to the bisectional plane.
c Torsion angle $\mathrm{C}(4) \mathrm{C}(3) \mathrm{CO}$ was adopted as the one-half value of the dihedral angle between $\mathrm{C}(4) \mathrm{C}(3) \mathrm{O}$ and $\mathrm{HC}(3) \mathrm{O}$, and the geometry of the methyl moiety was assumed to be of the exact staggered form.
${ }^{d}$ Torsion angles $\mathrm{N}(1) \mathrm{C}(2) \mathrm{OC}$ and $\mathrm{N}(1) \mathrm{C}(2) \mathrm{SC}$ were adopted as the one-half value of the dihedral angle between $\mathrm{N}(1) \mathrm{C}(2) \mathrm{B}$ and $\mathrm{HC}(2) \mathrm{B}$, the geometries of Me moieties of the OMe and SMe groups were assumed to be the exact staggered forms, and the torsion angle $\mathrm{C}(2) \mathrm{SCC}$ of the $\mathrm{SCH}=\mathrm{CH}_{2}$ group was assumed to be equal to $0^{\circ}$.

Fig. 1. Relationships between $\beta$-lactam $\nu_{\mathrm{C}=0}$ and $\cos \theta$.

 pressed if $\theta$ increases. The increase in $\theta$ strengthens the double-bond character of the $\beta$-lactam
carbonyl group, causing a shift to a higher wavenumber of $\nu_{\mathrm{C}=0}$. Since an excellent linear relationship (correlation coefficient, $\mathrm{r}=1.00$ ) was found between $\cos \theta$ and the $\pi$-bond order of the $\beta$-lactam $\mathrm{C}=\mathrm{O}$ bond obtained by the $\mathrm{CNDO} / 2$ calculation in the model molecule (I) shown in Table 2, the experimental $\nu_{\mathrm{C}=0}$ values were plotted against $\cos \theta$. As shown in Fig. 1, the plots give good linear relationships. This suggests that the effect of the change in $\theta$ is more important than any other electronic effect due to an atom at the 1 -position, a $7 \alpha$-methoxy group, and a $\Delta^{3}$ double bond.

We found that the substitution of the $7 \alpha$ hydrogen atom by a methoxy group is attended by a decrease in torsion angle $\phi_{1}$. This may be ascribed to a decrease in $\theta$ in the $7 \alpha$-methoxysubstituted compounds, because the repulsion increases between a $7 \beta$-amide group and an atom at the 1 -position, causing transformation of the six-membered ring. This repulsion influences the geometry of the $7 \beta$-amide group. As expected, the amide $\nu_{\mathrm{c}=0}$ shifts to a higher wavenumber with

Table 3. Bond energies of $\mathrm{C}=\mathrm{O}$ bond ( $\mathrm{E}_{\mathrm{C}=0}$ ) and $\pi$-electron densities on the carbon atom of $\mathrm{C}=\mathrm{O}$ bond ( $\mathrm{D}_{\pi}$ ) by $\mathrm{CNDO} / 2$ calculations in model molecules (I)~(IV).

| Compound | $\mathrm{E}_{\mathrm{C}=0}(\mathrm{I})$ <br> a.v. | $\mathrm{E}_{\mathrm{C}=0}(\mathrm{II})$ <br> a.v. | $\mathrm{E}_{\mathrm{C}=0}(\mathrm{III})$ <br> a.v. | $\mathrm{E}_{\mathrm{C}=0}(\mathrm{IV})$ <br> a.v. | Compound | $\mathrm{D}_{\pi}(\mathrm{I})$ | $\mathrm{D}_{\pi}(\mathrm{II})$ | $\mathrm{D}_{\pi}(\mathrm{III})$ | $\mathrm{D}_{\pi}(\mathrm{IV})$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathbf{1}$ | 1.60631 | 1.60805 | 1.60805 | 1.60568 | $\mathbf{1 7}$ | 0.79532 | 0.79802 | 0.79802 | 0.79933 |
| $\mathbf{2}$ | 1.60438 | 1.60643 | 1.60643 | 1.60414 | $\mathbf{1 8}$ | 0.79661 | 0.79988 | 0.79988 | 0.80185 |
| $\mathbf{3}$ | 1.60456 | 1.60667 | 1.60249 | 1.60089 | $\mathbf{1 9}$ | 0.79618 | 0.79970 | 0.80767 | 0.80780 |
| $\mathbf{4}$ | 1.60335 | 1.60535 | 1.60128 | 1.59947 | $\mathbf{2 0}$ | 0.79688 | 0.79993 | 0.80810 | 0.80948 |
| $\mathbf{6}$ | 1.60249 | 1.60249 | 1.60249 | 1.60285 | $\mathbf{2 2}$ | 0.79699 | 0.79699 | 0.79699 | 0.79969 |
| $\mathbf{8}$ | 1.60213 | 1.60213 | 1.59829 | 1.59858 | $\mathbf{2 4}$ | 0.79657 | 0.79657 | 0.80459 | 0.80658 |
| $\mathrm{r}^{a}$ | 0.96 | 0.89 | 0.95 | 0.86 |  | 0.70 | 0.01 | 0.75 | 0.83 |

a Correlation coefficient of relationships between $\mathrm{E}_{\mathrm{C}}^{1 / 2}=\mathrm{o}$ and $\beta$-lactam $\nu_{\mathrm{C}=0}$ and $\mathrm{D}_{\pi}$ and $\delta_{\mathrm{C}}$ of the corresponding compounds shown in Table 1.
increasing torsion angle $\left|\phi_{2}\right|$, when the $7 \alpha$-hydrogen atom is substituted by a methoxy group. The increase in $\left|\phi_{2}\right|$ suppresses the resonance in the amide moiety, and therefore strengthens the double-bond character of the amide $\mathrm{C}=\mathrm{O}$.

The CNDO/2 calculations were carried out using the program of Pople and Beveridge ${ }^{12}$ ). On the basis of the available electron-diffraction and X-ray analysis data on analogous compounds ${ }^{8,7 \sim 1,13 \sim 15)}$, we adopted the geometries of model molecules (I) $\sim(I V)$ shown in Table 2. For the calculations for molecules (I) $\sim(I V)$, the $\theta$, the $\theta$ and Y , the $\theta, \mathrm{Y}$, and X , and the $\theta, \mathrm{Y}$, X , and B listed in Table 1 were taken into account, respectively; here, Y is $\mathrm{CH}=\mathrm{CH}_{2}$ for $\mathbf{1 \sim 4}$ and $\mathrm{CH}_{3}$ for $\mathbf{6}$ and $\mathbf{8}$; X is H for $\mathbf{1 , 2}$, and $\mathbf{6}$ and $\mathrm{OCH}_{3}$ for $\mathbf{3 , 4} 4$ and $\mathbf{8}$; and B is $\mathrm{OCH}_{3}$ for $\mathbf{1}$ and $\mathbf{3}, \mathrm{SCH}_{3}$ for $\mathbf{2}$ and $\mathbf{4}$, and $\mathrm{SCH}=\mathrm{CH}_{2}$ for 6 and 8. The $\mathrm{E}_{\mathrm{C}=0}$ and $\mathrm{D}_{\pi}$ values obtained from the $\mathrm{CNDO} / 2$ calculations are given in Table 3, where $\mathrm{E}_{\mathrm{o}=\mathrm{o}}$ is the bond energy of the $C=O$ bond and $D_{\pi}$ is the $\pi$-electron density on the carbon atom of the $\mathrm{C}=\mathrm{O}$ bond. When the potential energy is represented by the Morse function, the force constant is proportional to the dissociation energy. Because the dissociation energy of the $\mathrm{C}=\mathrm{O}$ bond is primarily proportional to the $\mathrm{E}_{\mathrm{C}=0}$, the $\mathrm{E}_{\mathrm{C}=0}^{1 / 2}$ is proportional to the $\nu_{\mathrm{C}=0}$. According to Pople's theory ${ }^{18)}$, the ${ }^{13} \mathrm{C}$ chemical shift, $\delta_{\mathrm{C}}$, is primarily proportional to the $\pi$-electron density. Thus, regression analysis was carried out between the $\beta$-lactam $\nu_{\mathrm{C}=0}$ and $\mathrm{E}_{\mathrm{C}}^{1 / 2}=0$ values and between the $\delta_{\mathrm{C}}$ of $\mathrm{C}(8)$ and $\mathrm{D}_{\pi}$ values. The correlation coefficients, r, obtained are given in Table 3. The r values of the $\beta$-lactam $\nu_{\mathrm{C}=0}$ vs. $\mathrm{E}_{\mathrm{C}=0}^{1 / 2}$ correlations are more than 0.86 for all model molecules (I)~ (IV). This suggests theoretically that the change
in $\beta$-lactam $\nu_{\mathrm{C}=0}$ is primarily governed by $\theta$, as pointed out experimentally above. However, the r values of the $\delta_{\mathrm{C}}$ vs. $\mathrm{D}_{\pi}$ correlations are respectively $0.70,0.01,0.75$ and 0.83 for model molecules (I) $\sim(\mathrm{IV})$. This suggests that the electronic effects due to the X and B moieties are of importance in this case. These results should be useful when considering the antibacterial reactivity of $\beta$-lactam ring in cephem derivatives ${ }^{\beta}$.

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